



Измерение спектральной функции τ -лептона
в распаде $\tau^- \rightarrow K^- K_S^0 \nu_\tau$ в эксперименте BaBar













С. Середняков, В. Дружинин

Экспериментальный семинар ИЯФ,
22 июня 2018 г.



Fundamental particles

Matter \downarrow $s=1/2$ Field \downarrow $s=1$

	1st gen.	2nd gen.	3rd gen.
Q U A R K	 <i>u</i> up	 <i>c</i> charm	 <i>t</i> top
	 <i>d</i> down	 <i>s</i> strange	 <i>b</i> bottom
L E P T O N	 <i>ν_e</i> <i>e neutrino</i>	 <i>ν_μ</i> <i>μ neutrino</i>	 <i>ν_τ</i> <i>τ neutrino</i>
	 <i>e</i> electron	 <i>μ</i> muon	 <i>τ</i> tau



Flavors

gluon

photon

$r < 10^{-17}$ cm !

Z boson

W boson

$s=0$ 125 GeV

+3 colours for each quarks

3 generations
+ antiparticles

Total number : 60 + H = 61

All have spin excl H

$M(\text{matter}) \sim 550 \text{ GeV}$

$\Sigma Q(\text{quarks}) = - \Sigma Q(\text{leptons}) !$

Что такое спектральная функция (SF); $\tau^- \rightarrow K^- K_S^0 \nu_\tau$

$$V(m) = 2 \frac{1}{N} \frac{dN}{dm} \frac{1}{m(M_\tau^2 - m^2)^2 (M_\tau^2 + 2m^2)} \frac{B(\tau \rightarrow K_S K \nu)}{B(\tau \rightarrow e \nu \nu)} \frac{M_\tau^6}{12\pi V_{ud}^2}$$

$V(m)$ описывает спектр масс адронов в распаде τ : $dN/dm (K^- K_S)$

Согласно CVC SF связывает спектр масс dN/dm с сечением e^+e^-

$$V(m) = \frac{m^2}{4\pi^2 \alpha^2} \sigma_{e^+e^- \rightarrow K \bar{K}(I=1)}(m)$$

Мотивация данной работы:

✓ Измерение спектральной функции (SF) в распаде $\tau^- \rightarrow K^- K_S \nu_\tau$

✓ Используя CVC и SF получить изовекторный вклад в сечение $e^+e^- \rightarrow K Kbar (I=1)$



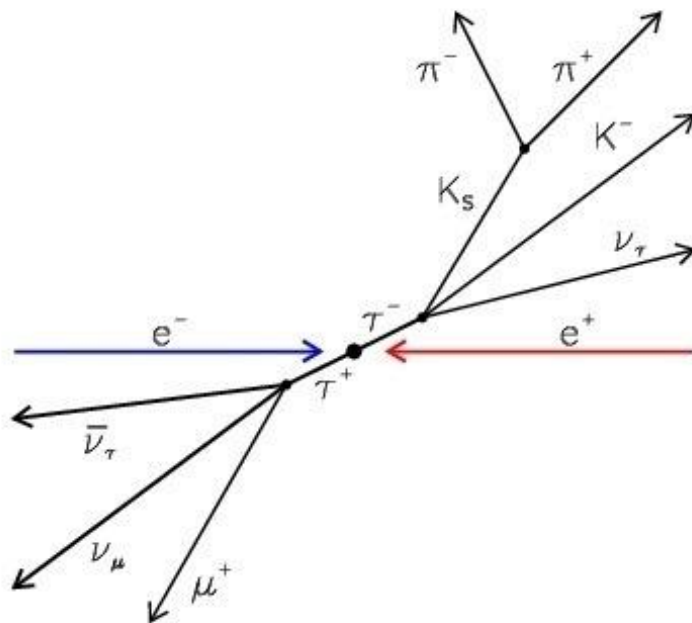
✓ Сравнить расчетные изовекторные вклады от e^+e^- и τ для процессов $e^+e^- \rightarrow K Kbar (I=1)$

✓ Корректировка массового спектра в MC генераторе $\tau \rightarrow K^- K_S \nu_\tau$

τ – lepton production at BaBar

$$e^+e^- \rightarrow \tau^+ \tau^-$$

$$E_{\text{c.m.}} = m(Y(4S)) = 10.58 \text{ GeV}$$



$$\sigma_{\tau\tau} = 0.92 \text{ nb}$$

$$L \approx 0.5 \text{ ab}^{-1}$$

$$N_{\tau\tau} \approx 10^9$$

τ Branching Ratios (PDG 2016)

$$\begin{aligned} \text{BR}(\tau^- \rightarrow K_S K^- \nu_\tau) &= 0.740 \pm 0.025 \cdot 10^{-3} \\ \text{BR}(\tau^- \rightarrow K_S \pi^- \nu_\tau) &= 4.2 \pm 0.07 \cdot 10^{-3} \\ \text{BR}(\tau^- \rightarrow K_S K^- \pi^0 \nu_\tau) &= 0.75 \pm 0.04 \cdot 10^{-3} \\ \text{BR}(\tau^- \rightarrow K^- \nu_\tau) &= 0.696 \pm 0.01 \% \\ \text{BR}(\tau^- \rightarrow \pi^- \nu_\tau) &= 10.82 \pm 0.05 \% \end{aligned}$$

τ Branching Ratio in MC

$$\text{BR}(\tau^- \rightarrow K_S K^- \nu_\tau) = 0.8255 \cdot 10^{-3}$$

11.5% difference !

CLEO $K^+K_S^-$ mass spectrum from τ decay.

CLEO Collab. Phys.Rev.D 53, 6037 (1996)

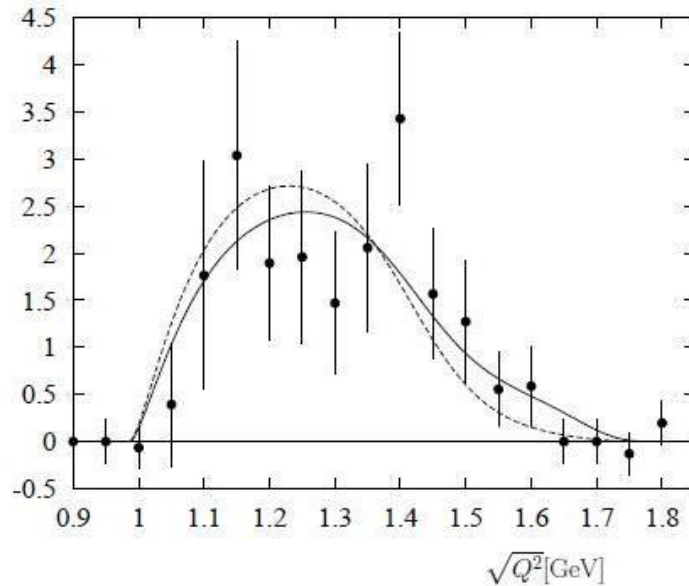


Figure 7: The normalized distribution $\frac{d\Gamma(\tau \rightarrow K^- K^0 \nu_\tau)/d\sqrt{Q^2}}{\Gamma(\tau \rightarrow K^- K^0 \nu_\tau)}$ in the kaon pair invariant mass $\sqrt{Q^2}$ in units of GeV^{-1} obtained from the fitted kaon form factor; the solid (dashed) line corresponds to the constrained (unconstrained) fit. The event distribution measured by CLEO Collaboration [45] and normalized, dividing by the total number of events, is shown with points.

DATA used in analysis

1. Run1-run6 - 468.3 fb⁻¹
kL=L_{MC} /Lrun
2. MC e⁺e⁻ → τ⁺τ⁻ , 816.3 fb⁻¹ , kL = 1.74
3. MC e⁺e⁻ → τ⁺τ⁻ → l⁺K_SK⁻ν_τ, 1088 fb⁻¹ , kL = 2.32
4. MC e⁺e⁻ → uds , 856 fb⁻¹ , kL= 1.83
5. MC e⁺e⁻ → c-cbar , 868.5 fb⁻¹ , kL= 1.85
6. MC e⁺e⁻ → B-Bbar, 1352.4 fb⁻¹ , kL= 2.89

Selection criteria

$$\tau_1 \rightarrow \text{KK}_S, \tau_2 \rightarrow e\nu\nu, \mu\nu\nu$$

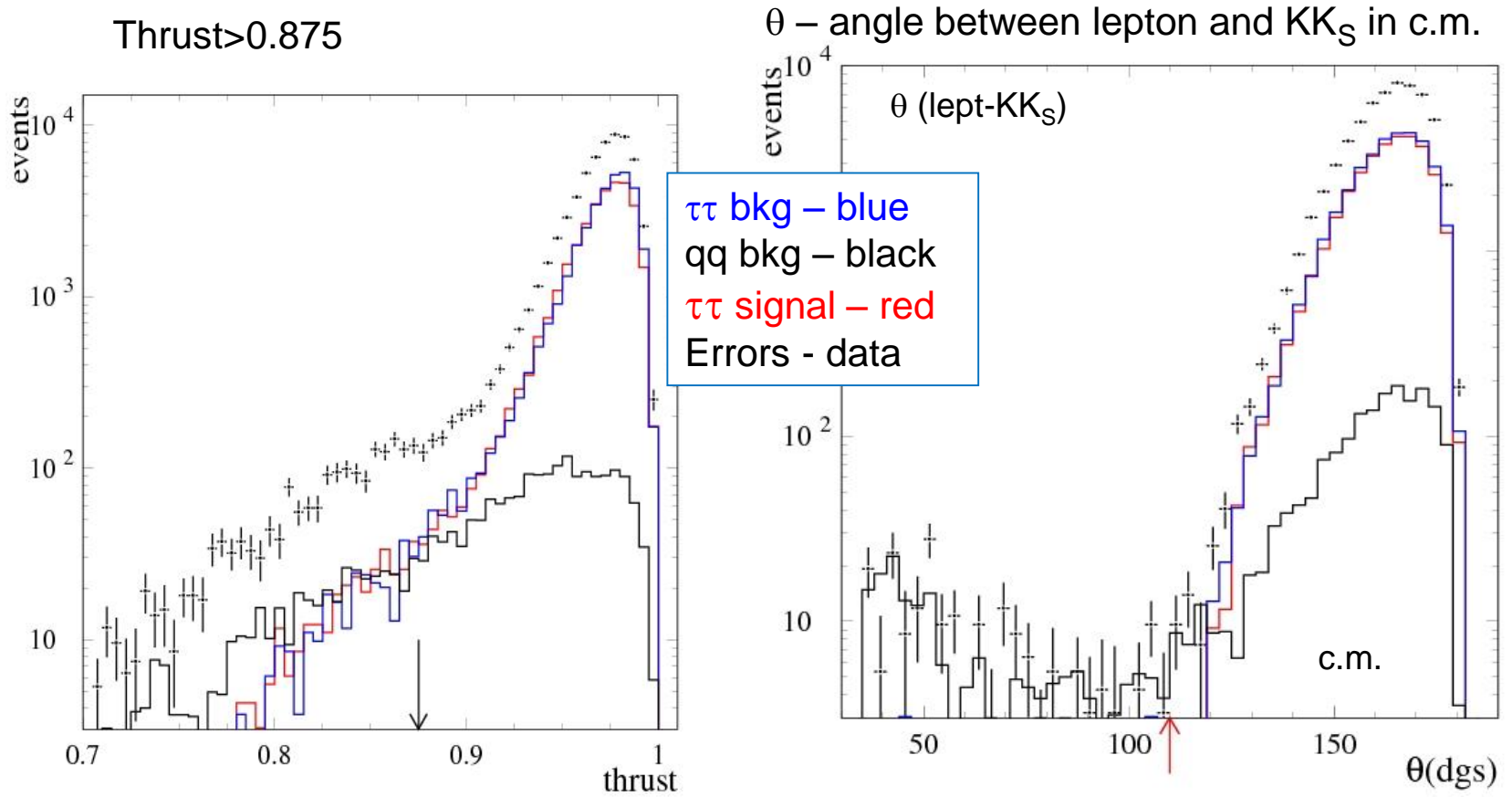
1. $N(\text{tracks})=4$,
2. $N(\text{K}_S)=1$, $\text{K}_S \rightarrow \pi^+\pi^-$
3. $N(\text{K}^\pm)=1$, $N(\mu)$.or. $N(e)=1$
4. $r_{\text{KS}} = 1 - 70 \text{ cm}$
5. $\text{thrust} > 0.875$
6. $\text{K}^\pm : p_{\text{lab}} = 0.4-5$,
7. $e, \mu : \cos\theta_{\text{lab}} < 0.9$, $p_{\text{lab}} > 1.2$, $p_{\text{cm}} < 4.5$
8. $\theta_{\text{CM}} > 110^\circ$, - angle lept. $\leftrightarrow \text{KK}_S$
9. $\Sigma E_\gamma < 2 \text{ GeV}$

Monte carlo selection of

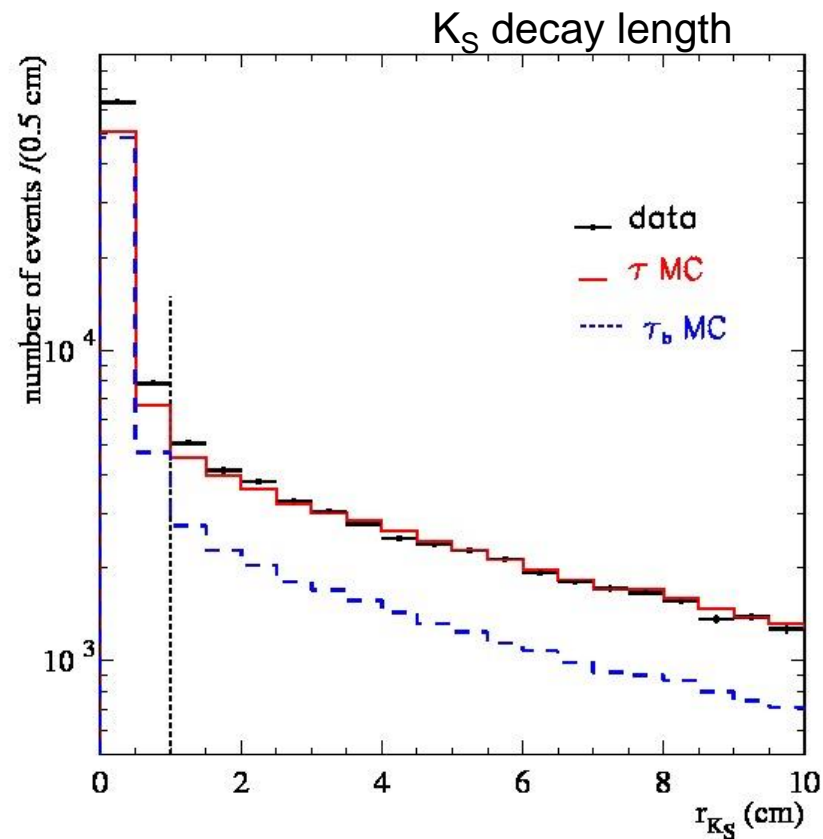
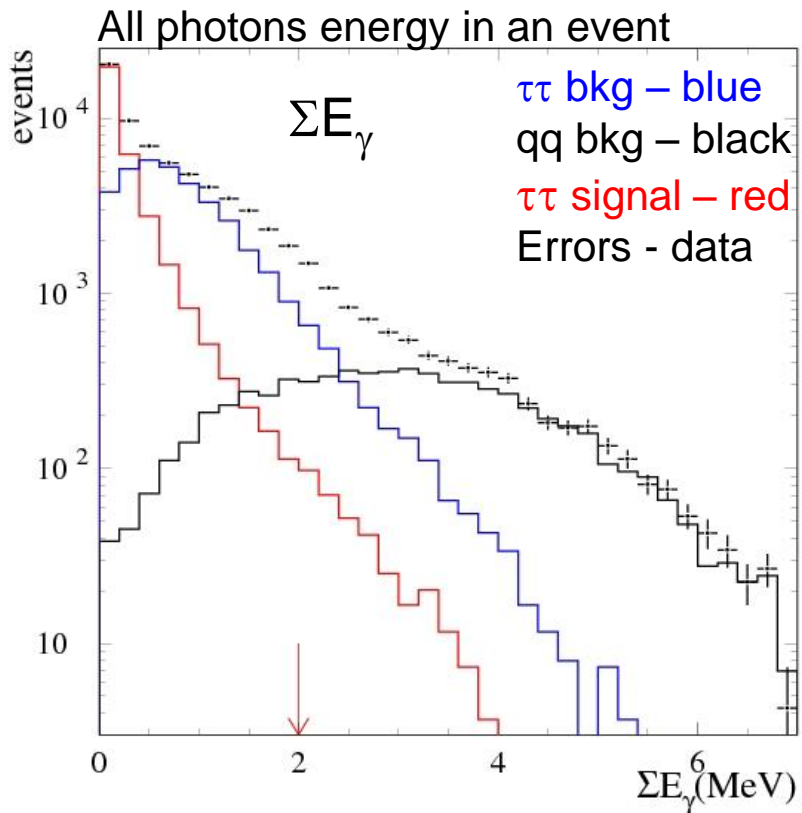
$\tau^+\tau^- \rightarrow l^+\text{K}_S\pi^-\nu_\tau$ mode :

1. $N(\text{K}_S)=1$, $N(\text{K}^\pm)=1$
2. $N(\mu)$.or. $N(e)=1$
3. $N(\pi^0)=0$, $N(\pi^\pm)=0$

Comments to selection conditions



Comments to selection conditions



Signal and background suppression - all cuts applied

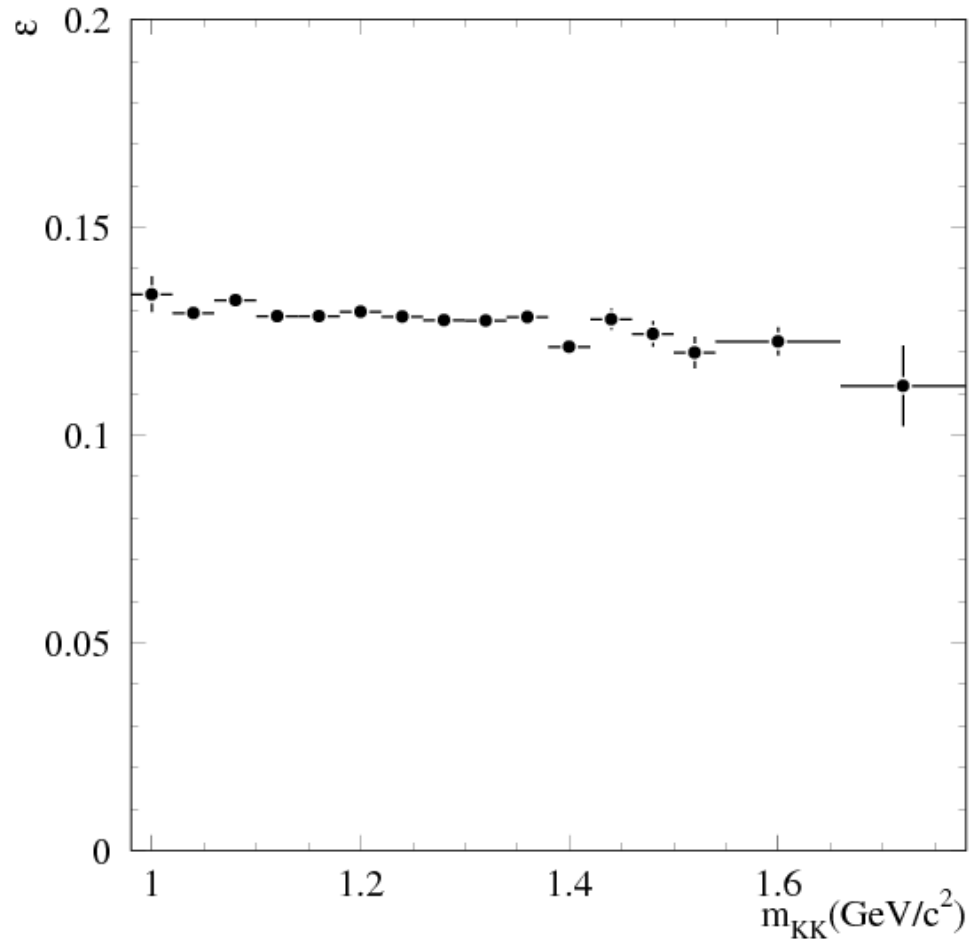
$\tau+\tau-(MC) \sim 7.5 \cdot 10^8 \text{ ev.} \rightarrow 1.2 \cdot 10^5 \text{ ev.} \text{ (} \sim 3.5 \text{ orders)}$

$udscb(MC) \sim 4.3 \cdot 10^9 \text{ ev.} \rightarrow 3.5 \cdot 10^3 \text{ ev.} \text{ (} \sim 6 \text{ orders)}$

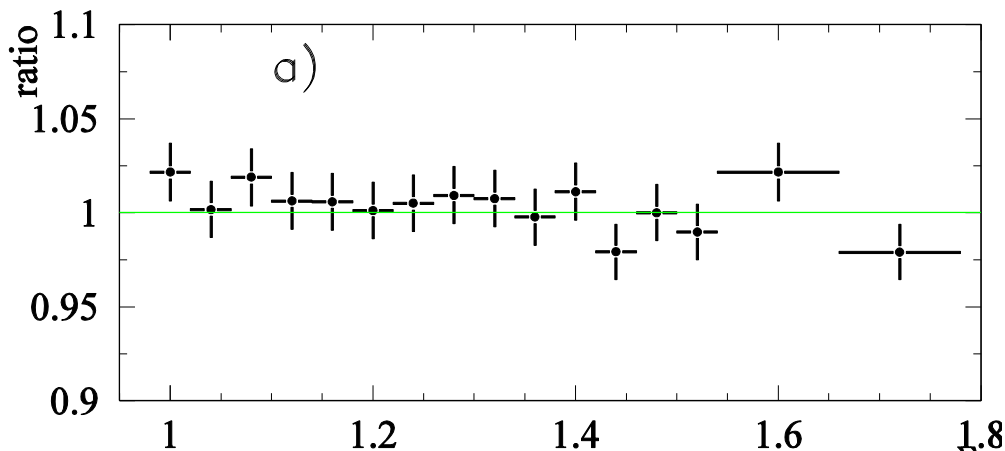
$\tau+\tau-(KK_S,MC) \sim 3 \cdot 10^5 \text{ ev.} \rightarrow 0.7 \cdot 10^5 \text{ ev} \text{ (} \sim 4 \text{ times)}$

$\text{data} \sim 4.2 \cdot 10^9 \text{ ev.} \rightarrow 1.4 \cdot 10^5 \text{ ev} \text{ (} \sim 4.5 \text{ order)}$

Detection efficiency vs KK_S mass – all cuts applied

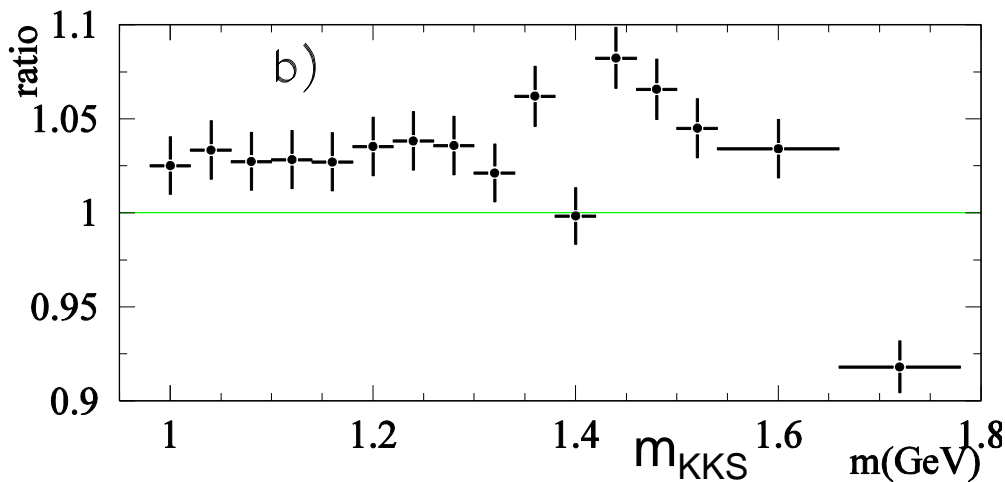


Data/MC efficiency corrections



- a) – signal $\tau \rightarrow KK_S \nu_\tau$
- b) – non $\tau \rightarrow KK_S \nu_\tau$

Used PID Tables from:
 muSelectorsMap(21)
 KselectorsMap(26)
 eSelectorsMap(8)

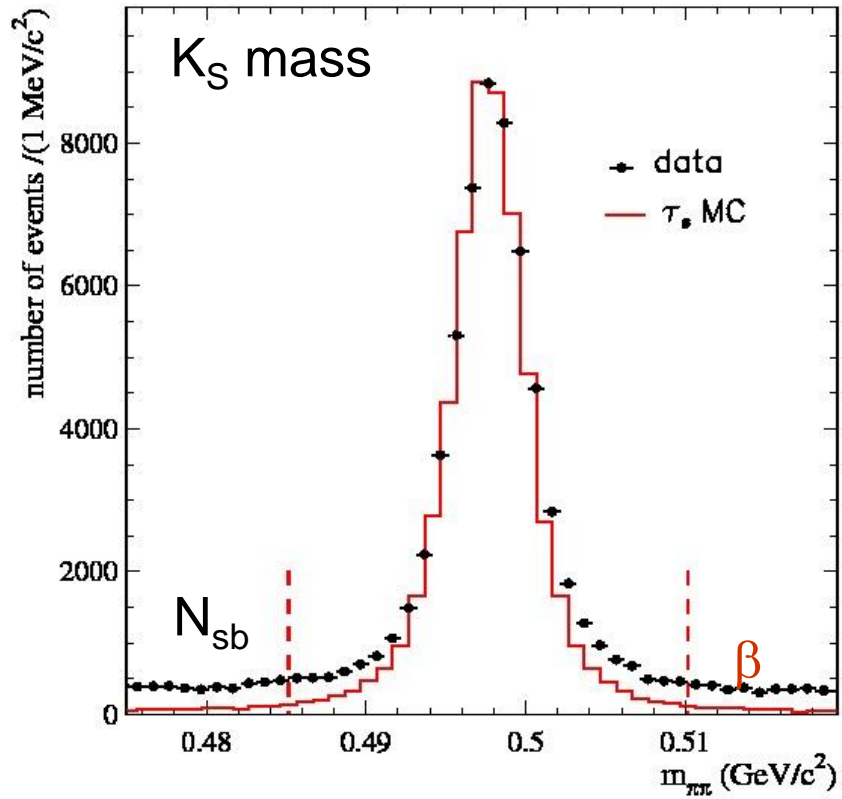


Corrected MC efficiencies:

$K \rightarrow K, \pi \rightarrow K$
 $\mu \rightarrow \mu, \pi \rightarrow \mu$
 $e \rightarrow e, \pi \rightarrow e$

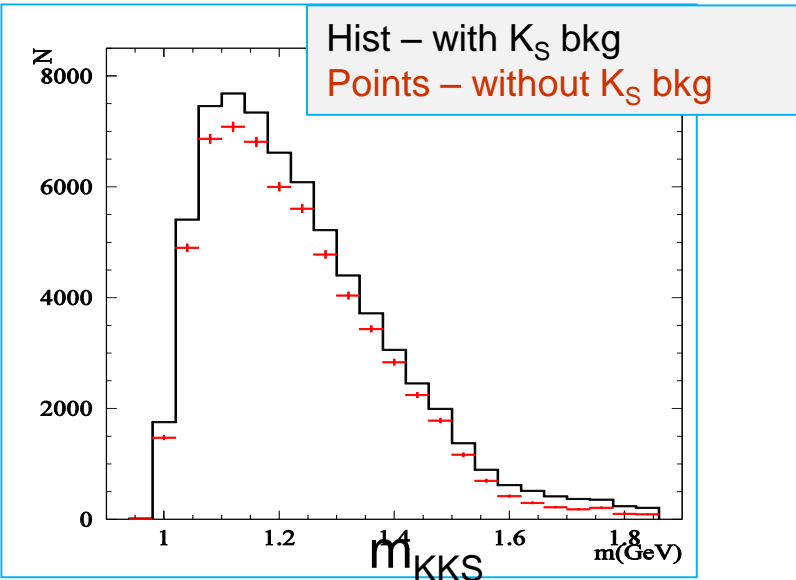
Corrections applied
 to value of ϵ
 in previous slide

K_S background subtraction



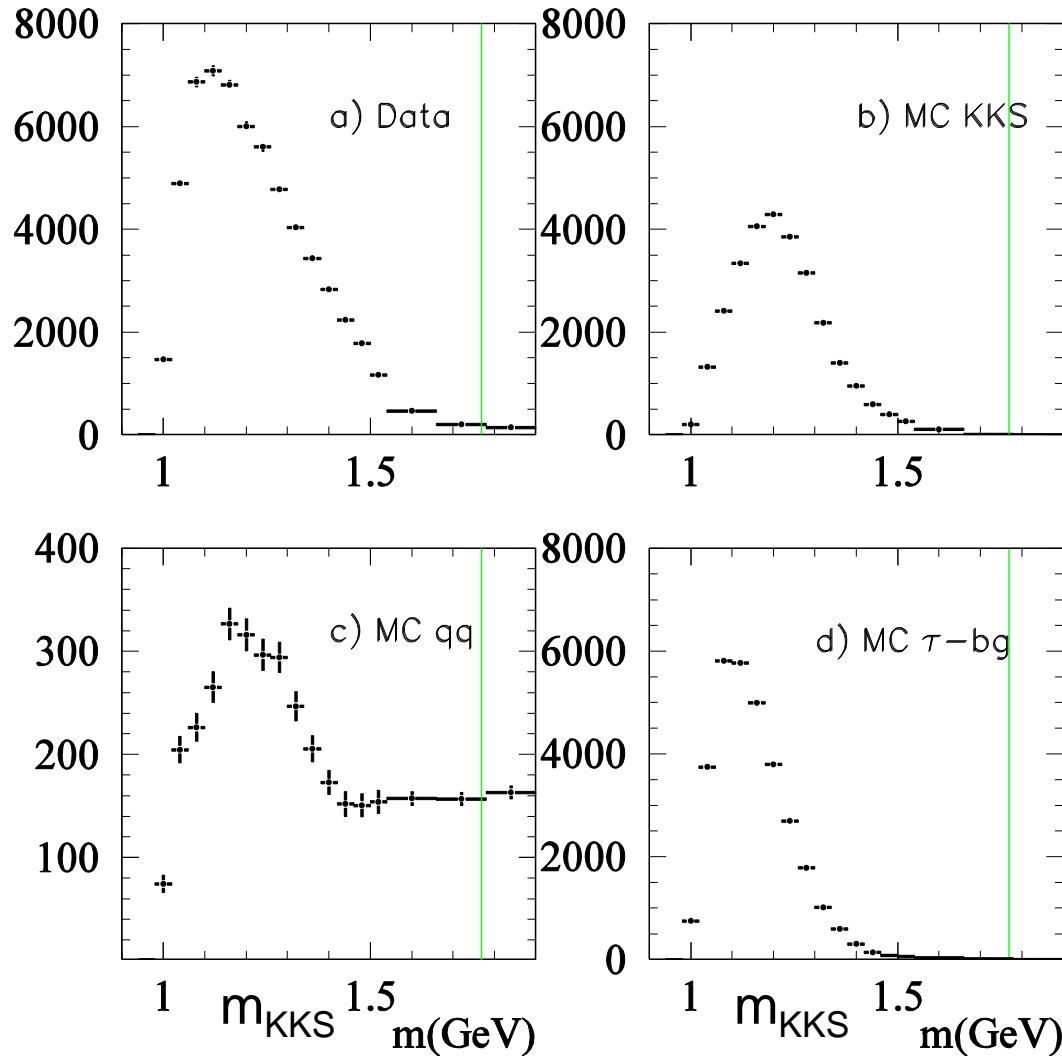
Δm=0.472-0.522=0.050 GeV

Effect of K_S background subtraction

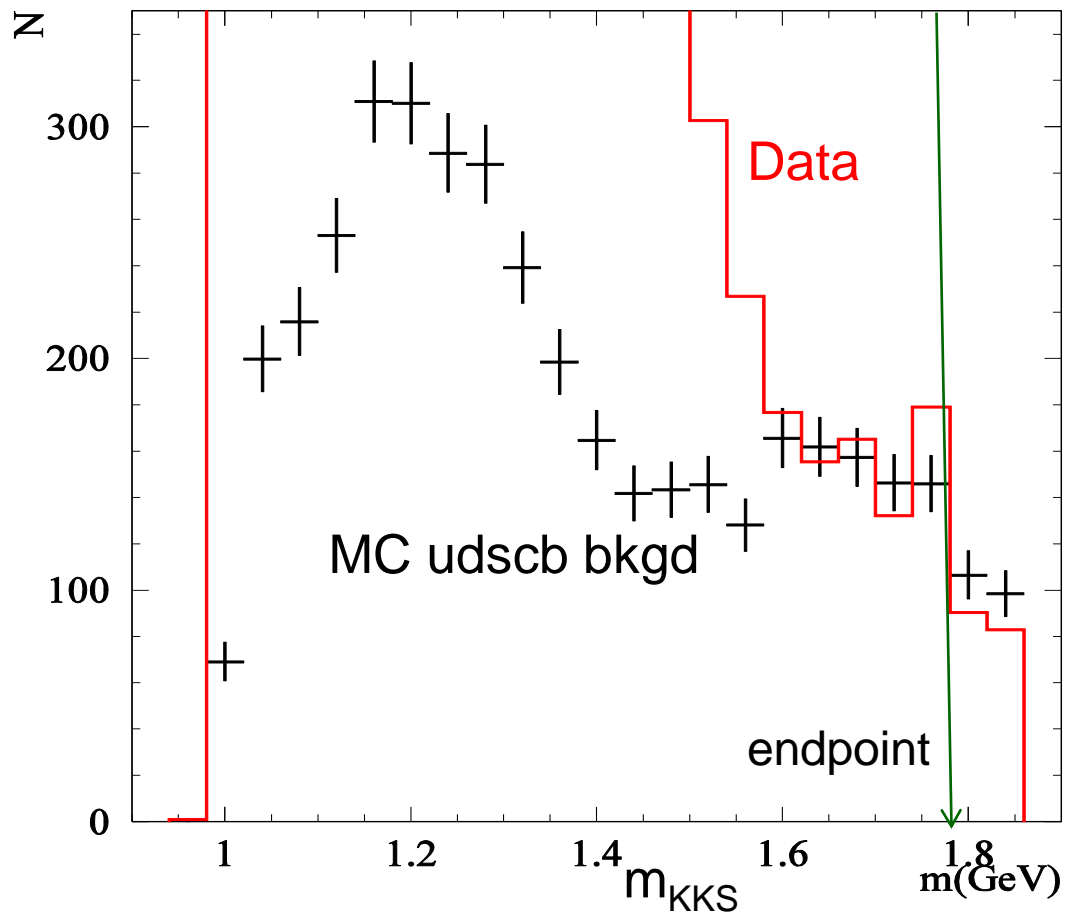


Sideband subtraction
 $N_{KS} = (\alpha N - N_{sb}) / (\alpha - \beta)$,
 $\alpha = 0.5, \beta = 0.0315$

KK_S mass spectra in data and MC after applying selection cuts. K_S bkgd subtracted

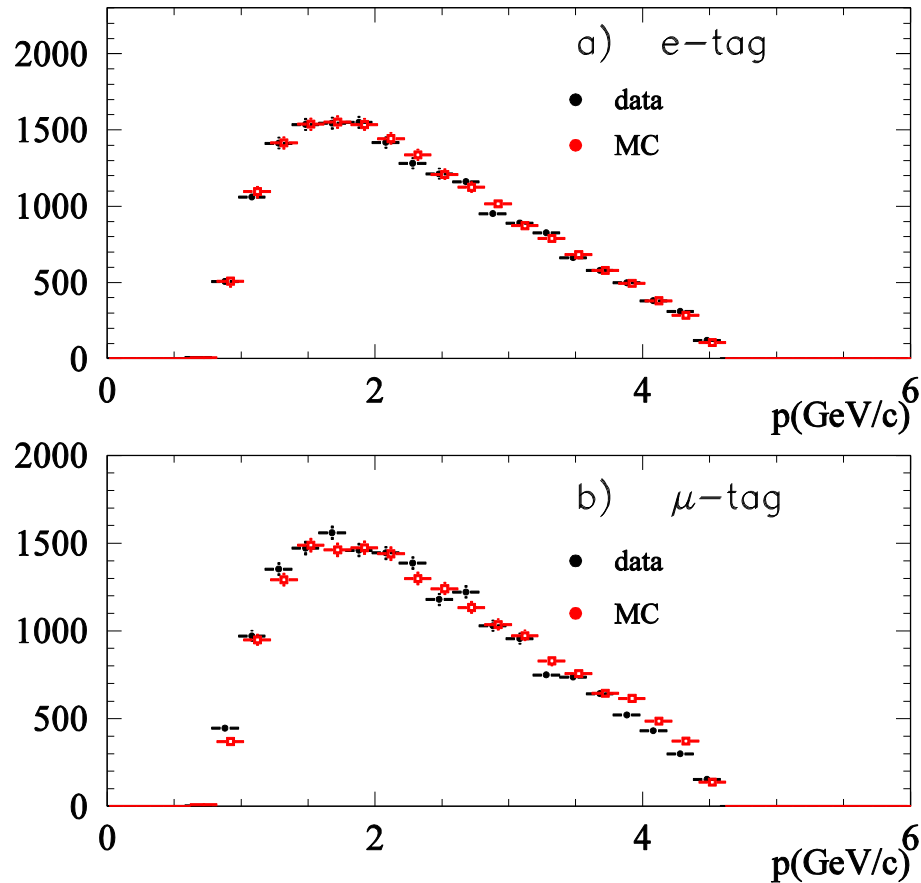


$q\bar{q}$ background contribution



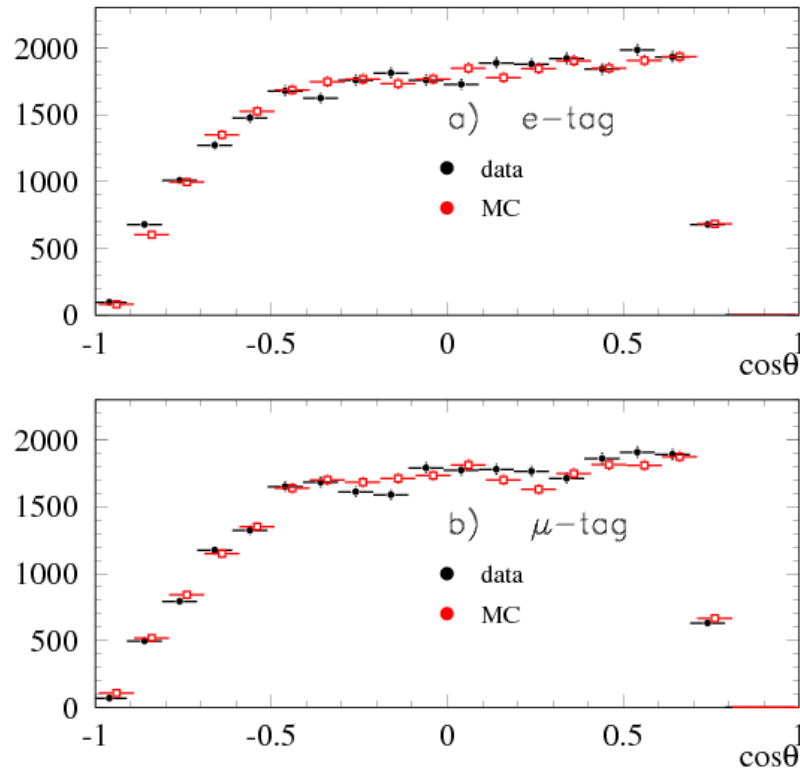
Data agree with MC near endpoint at $m(KK_S) \sim m(\tau)$!

Lepton CM momentum, data-MC comparison



$q\bar{q}$ background
subtracted from data

Leptons CM $\cos\theta$, data-MC comparison



$q\bar{q}$ background
subtracted from data

Distribution of selected events over subprocesses

Data events
number (69286 ev.)

Tau MC $\tau^+\tau^- \rightarrow l\bar{K}_S K^+$
events number (32341 ev.)

+

Tau MC $\tau^+\tau^- \rightarrow \text{non } l\bar{K}_S K^+$
events number (35441 ev.)

+

MC hadron bkgd
 $e^+e^- \rightarrow \text{udscb}$
events number (5382 ev.)

Structure of τ background

- | | | |
|----|--|--|
| 1. | $\tau^- \rightarrow K_S K^- \pi^0 \nu_\tau \sim 70\%$ | Background without π^0 , well measured, subtracted using MC |
| 2. | $\tau^- \rightarrow \pi^- K_S \nu_\tau \sim 10\%$ | |
| 3. | $\tau^- \rightarrow \pi^- K_S \pi^0 \nu_\tau \sim 6\%$ | Background with $\pi^0 \sim 80\%$, mass spectra not measured, subtracted using data |
| 4. | $\tau^- \rightarrow \pi^- \nu_\tau \sim 8\%$ | |
| 5. | $\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$ | |

Structure of qq background

uds $\sim 80\%$, cc $\sim 15\%$, bb $\sim 5\%$

Subtraction of π^0 background
 System of linear equations (in each KK_S mass bin)

Eq.1

$$N_{ex0} = (1 - \epsilon_S) N_{sig}^\tau + (1 - \epsilon_b) N_{bg}^\tau$$

$$N_{ex1} = \epsilon_S N_{sig}^\tau + \epsilon_b N_{bg}^\tau$$

$N_{\pi^0} = 0$,
 number of found π^0

$$N_{ex0} = N_{dt0} - N_{bg,0}^{\tau,0} - N_{qq0}$$

$$N_{ex1} = N_{dt1} - N_{bg,1}^{\tau,0} - N_{qq1}$$

Eq.2

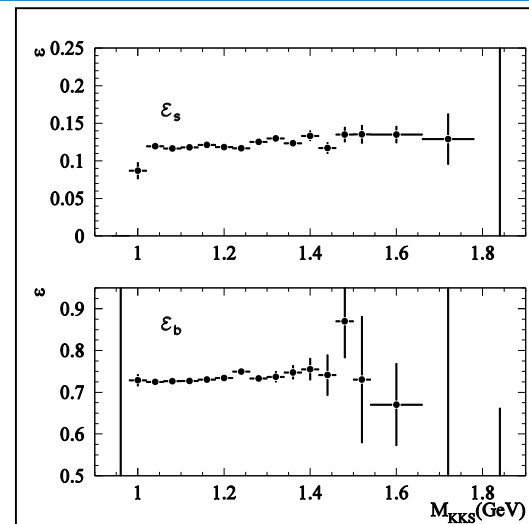
$$\epsilon_S = N_{sig,1}^{\tau,0} / (N_{sig,1}^{\tau,0} + N_{sig,0}^{\tau,0})$$

$$\epsilon_b = N_{bg,1}^{\tau>0} / (N_{bg,1}^{\tau>0} + N_{bg,0}^{\tau>0})$$

Eq.3

Solution of linear equations gives the
 signal (N_{KS}^τ) and background (N_{bg}^τ)
 KK_S mass spectra

From MC



Correction to π^0 efficiency:

$$\delta\epsilon = 1 - (0.024 \pm 0.08) =$$

$$= 0.976 \pm 0.008$$

(BAD 2621)

$\epsilon_S \neq 0$

Extraction of KKS mass spectrum from the system of linear equations (in each KK_S mass bin)

Eq.1

$$N_{ex0} = (1 - \epsilon_S) N_{sig}^\tau + (1 - \epsilon_b) N_{bg}^\tau$$

$$N_{ex1} = \epsilon_S N_{sig}^\tau + \epsilon_b N_{bg}^\tau$$

Solution of linear equations gives the signal (N_{KS}^τ) and background (N_{bg}^τ) KK_S mass spectra

Correction to π^0 efficiency:

$$\begin{aligned} \delta\epsilon &= 1 - (0.024 \pm 0.008) = \\ &= 0.976 \pm 0.008 \\ &\text{(BAD 2621)} \end{aligned}$$

$$\epsilon_S \neq 0$$

$N_{\pi^0} = 0$,
number of found π^0

Eq.2

$$\begin{aligned} N_{ex0} &= N_{dt0} - N_{bg,0}^{\tau,0} - N_{qq0} \\ N_{ex1} &= N_{dt1} - N_{bg,1}^{\tau,0} - N_{qq1} \end{aligned}$$

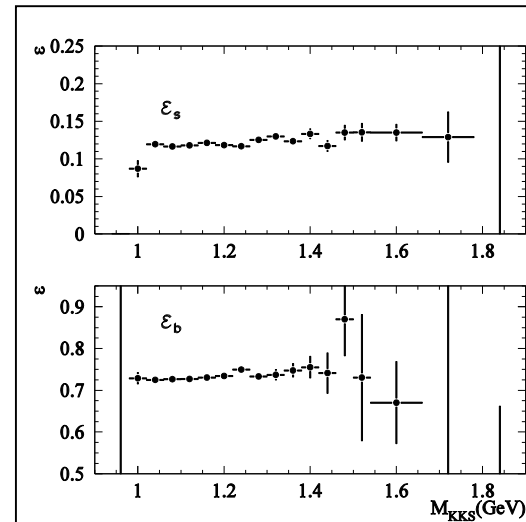
$N_{\pi^0} > 0$,

$$\epsilon_S = N_{sig,1}^{\tau,0} / (N_{sig,1}^{\tau,0} + N_{sig,0}^{\tau,0})$$

$$\epsilon_b = N_{bg,1}^{\tau>0} / (N_{bg,1}^{\tau>0} + N_{bg,0}^{\tau>0})$$

Eq.3

From MC



Subtraction of π^0 background

Structure of π^0 background

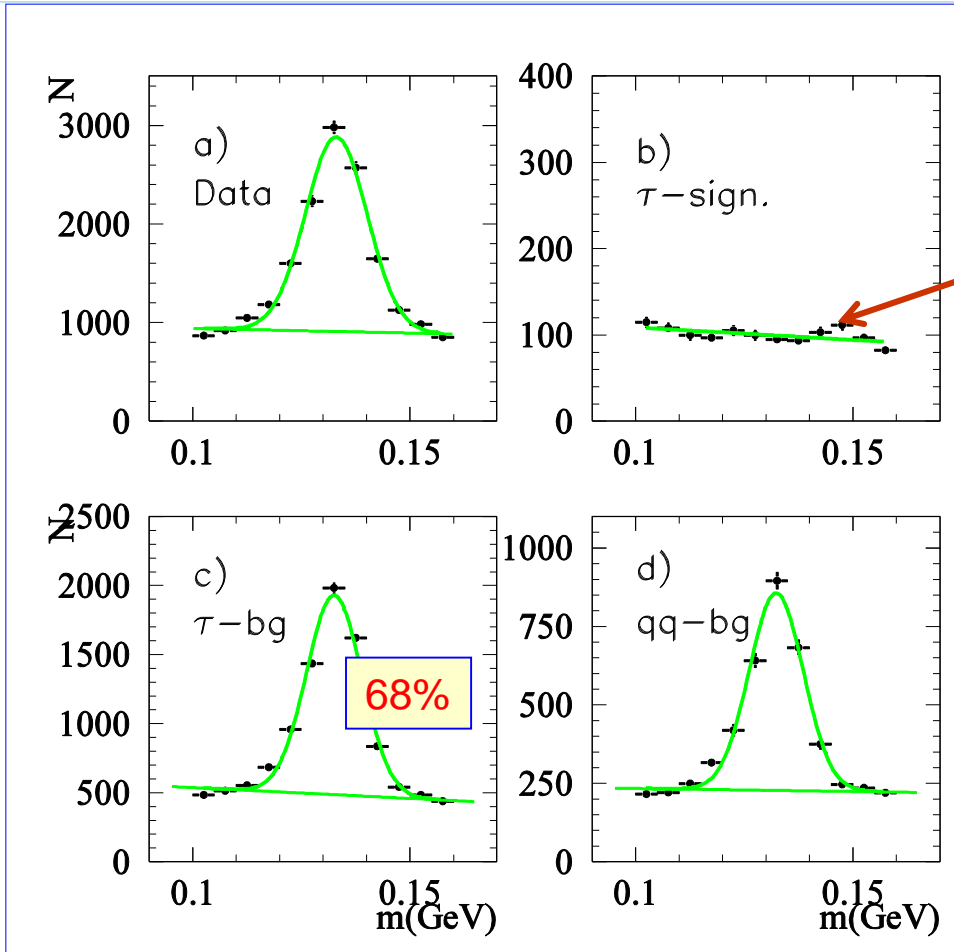
π^0 spectra for sum of events in all Δm bins

$$M(\pi^0) = M_{\gamma\gamma} = 100-160 \text{ MeV}$$

Fitting gives:

$$N_{\pi^0} = N_{\text{GAUSS}} + N_{\text{RANDOM}}$$

Only N_{RANDOM}



68% - is the part of events with true π^0 in τ background

Split lower line in Eq.1 p.24 (for sum of events)

Transformation of lin.equations

$$N_{\text{ex0}} = (1 - \varepsilon_S) N_{\text{sig}}^\tau + (1 - \varepsilon_b) N_{\text{bg}}^\tau$$

$$N^0_{\text{ex1}} = \varepsilon_S N_{\text{sig}}^\tau + 0.32 \cdot \varepsilon_b N_{\text{bg}}^\tau$$

Without true π^0

$$N^*_{\text{ex1}} = \dots\dots\dots 0.68 \cdot \varepsilon_b N_{\text{bg}}^\tau$$

With true π^0

Corrections to background subtraction (for sum of events in all Δm bins)

Ideal equation system

$$N_{ex0}^* = N_{sig}^\tau + (1 - \epsilon_b^*) N_{bg}^\tau$$

$$N_{ex1}^* = \epsilon_b^* N_{bg}^\tau$$

N_{ex0}^* – events without π^0 + lin. background

N_{ex1}^* – events with π^0 from Gaussian fit to the π^0 spectrum only

$$N_{sig}^\tau \text{ (modified)} = 1.01 N_{sig}^\tau \text{ (p.24)}$$

$$\epsilon_s^* = 0!$$

$$\epsilon_b^* \rightarrow 0.68 * 0.72 = 0.49$$

Fraction of events with π^0

ϵ_b

Return to eq,1 p.24 with division into KK_S mass bins with corrected efficiencies

$$N_{\text{ex0}} = (1 - \varepsilon'_S) N_{\text{sig}}^\tau + (1 - \varepsilon'_b) N_{\text{bg}}^\tau$$

$$N_{\text{ex1}} = \varepsilon'_S N_{\text{sig}}^\tau + \varepsilon'_b N_{\text{bg}}^\tau$$

Corrected efficiencies:

$\varepsilon'_S \rightarrow \varepsilon_S (1.05 \pm 0.05)$

$\varepsilon'_b \rightarrow \varepsilon_b 0.984$

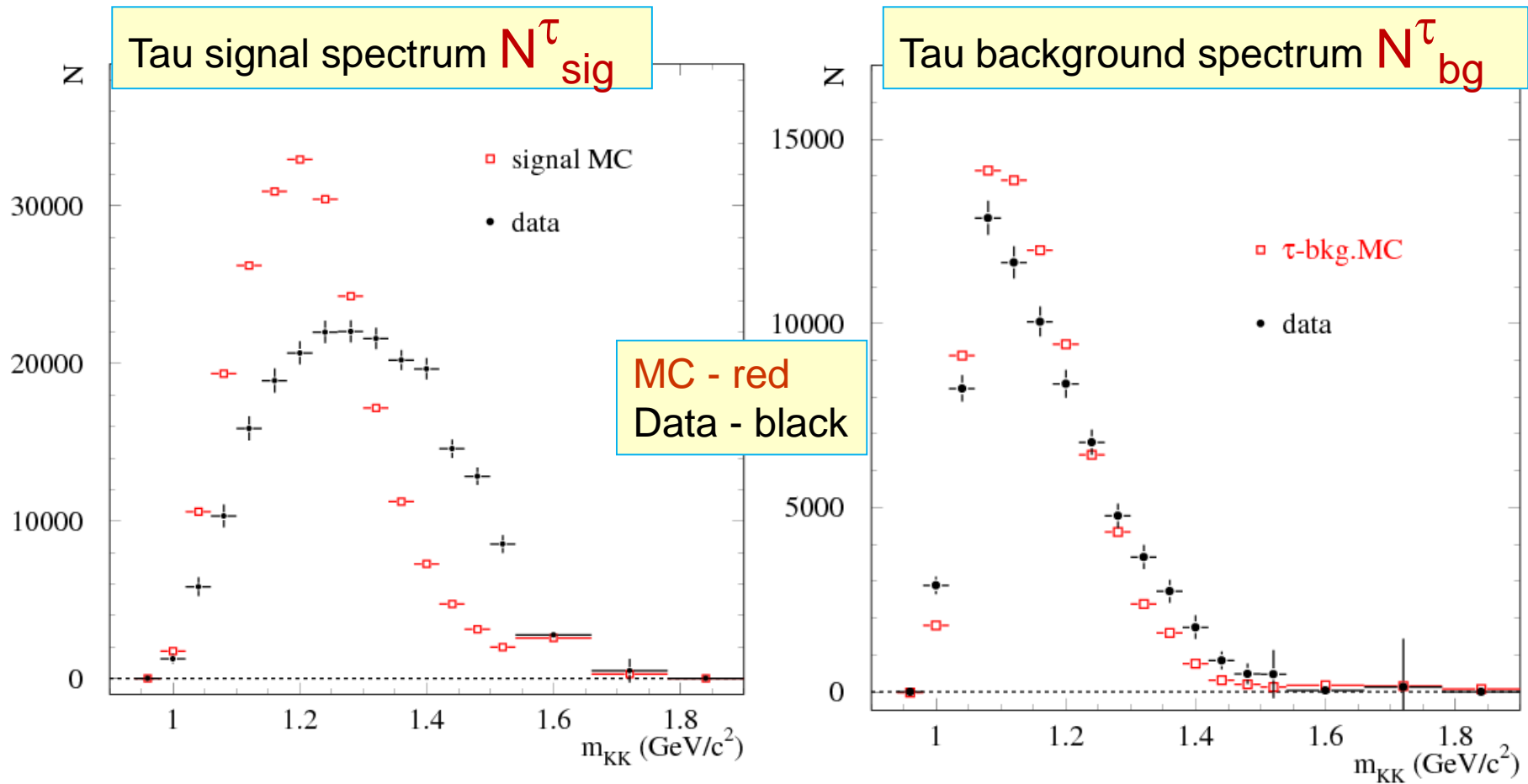
- π^0 efficiency correction

- spurious photon correction

- $0.984 = 1 - 0.024 * 0.68$

Fraction of events with π^0

The final KK_S mass spectra for tau signal and background



Branching fraction $\text{BF}(\tau^- \rightarrow \text{KK}_S \nu_\tau)$

$$\text{BF} = \frac{N_{\text{exp}}}{\text{LB}_{\text{lep}} \sigma_{\tau\tau}} = 0.740 \pm 0.011 \times 10^{-3} (\text{stat}) \pm 0.021 \times 10^{-3} (\text{syst})$$

$N_{\text{exp}} = (223741 \pm 3461)$ - total number of signal events,

$L = 468 \pm 2.5$ inv.fb, $B_{\text{lep}} = 0.3521 \pm 0.0006$, $\sigma_{\tau\tau} = 0.919 \pm 0.003$ nb

Total error (stat+syst) = 3.2%

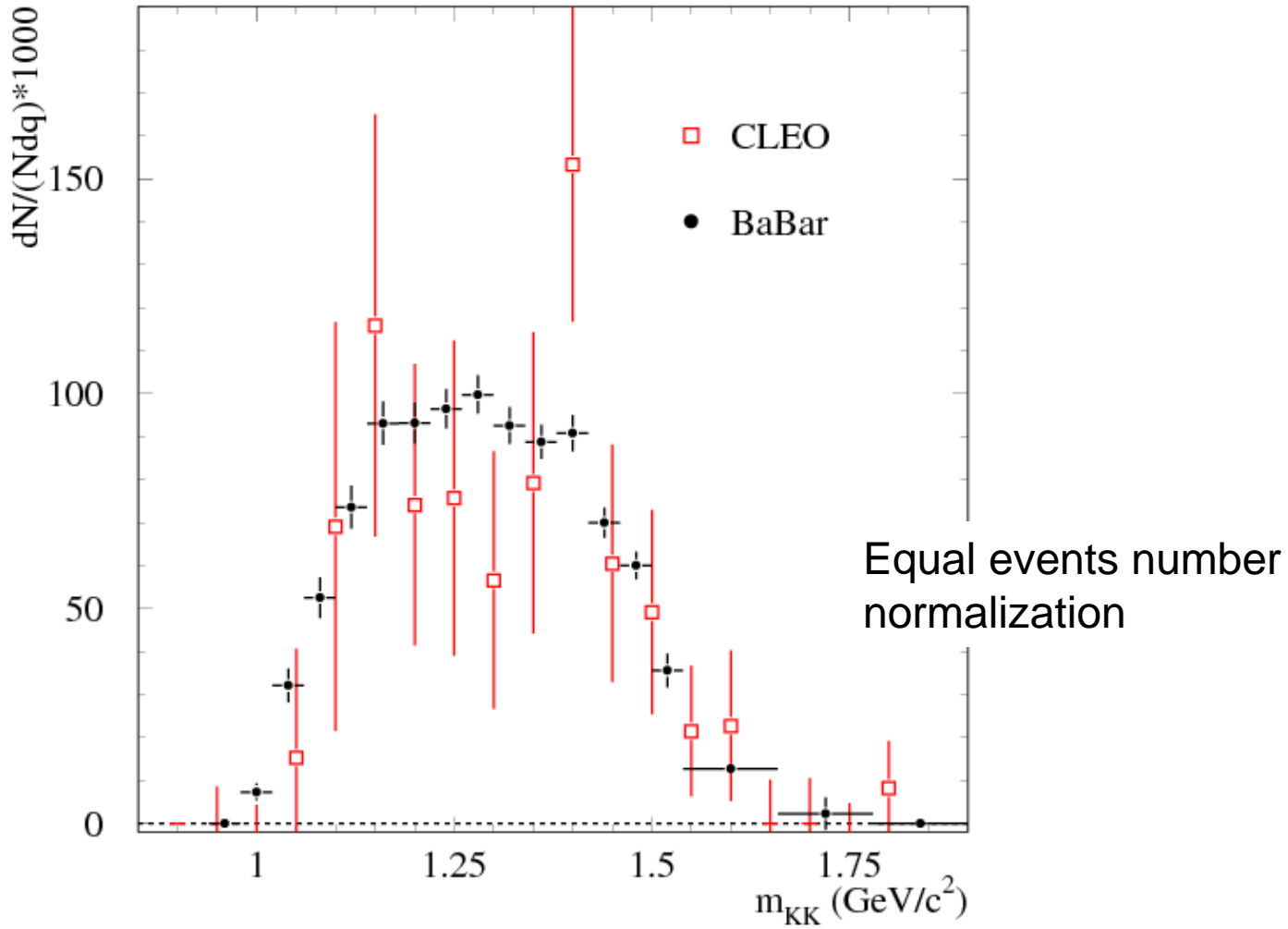
$\text{BF} (\text{PDG}_{2016}) = 0.740 \pm 0.025$

Summary of systematic to $\text{BF}(\tau^- \rightarrow K_S K^- \nu_\tau)$

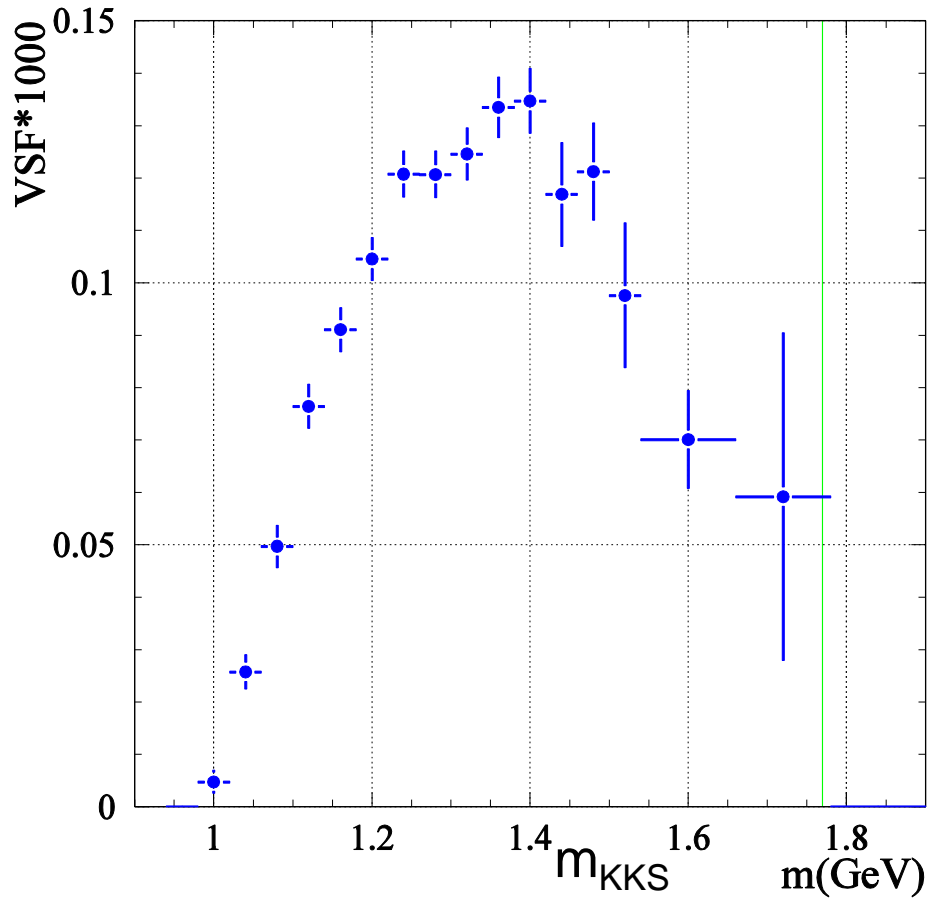
- 1 - K_S bkgd - 0.4%
- 2 - luminosity - 0.5%
- 3 - hadron bkgd subtr, - 0.5%
- 4 - track efficiency - 1.0%
- 5 - PID - 0.5%
- 6 - τ bkgd with π^0 - 2.3%
- 7 - τ bkgd without π^0 - 0.3%

Total - 2.7%

BaBar-CLEO KK_S mass spectra comparison



Vector spectral function for $\tau^- \rightarrow K_S K^- \nu_\tau$ process,
- first measurement



Заключение

1. В процессе $\tau^- \rightarrow K_S K^- \nu_\tau$ измерен массовый спектр $K_S K^-$ системы с точностью значительно лучше чем в предыдущих измерениях
2. Измеренная вероятность распада $\tau^- \rightarrow K_S K^- \nu_\tau$ хорошо согласуется со среднемировым значением
3. Впервые построена векторная спектральная функция распада $\tau^- \rightarrow K_S K^- \nu_\tau$.

To be submitted to Phys.Rev. D, rapid communication

